

Lecture 01 | Part 1

Welcome

machine learning ² magic

(demo)¹

¹Source code: https://gist.github.com/eldridgejm/b8cdac34bf77a4c3add9a9bf2d7362c8

machine learning ² magic

machine learning = math + data

But first...

The syllabus: dsc140a.com

Labs + Homeworks + Exams + "Super Homework"

- This class has some policies you may/may not be familiar with:
 - slip days
 - lab redemption
 - exam redemption

This Class

This course focuses on machine learning theory.
 80% theory, 20% practice

Other classes (DSC 80, DSC 148) focus on machine learning practice.

Math Background

- The most important prereqs for this class are:
 - DSC 40A (mathematical foundations of ML)
 - DSC 80 (ML practice + pandas)
 - MATH 20C (multivariable calculus)
 - MATH 18 (linear algebra)
 - MATH 183 (probability/statistics)
- We'll review some of the math, but you might want to fill in some gaps on your own.

If you're a DSC major/minor...

- There are several ways to satisfy the DSC major's ML requirement
 - CSE 150A, CSE 151A, DSC 140A, DSC 140B
- Recommendation: take DSC 140A and DSC 140B
- Avoid "mixing and matching"
 e.g., avoid DSC 140A + CSE 151A

If you're not a DSC major/minor...

Welcome!

- This class assumes that you've seen some machine learning before.
 least squares regression, gradient descent, empirical
 - risk minimization
- If not, DSC 40A might be a good place to start.
- You'll also want to be comfortable with Python.



Lecture 01 | Part 2

Prediction

Prediction

- Prediction is the most common task in machine learning.
 - **Given** some input information...
 - Predict some related output.

Examples

- Given a data scientist's age, college GPA, and state of residence, predict their salary.
- Given a penguin's bill length and body mass, predict its species.
- Given a digital image, predict the gesture being made.

Features and Labels

Each piece of input information is called a feature.

The output we're trying to predict is called the label (or target).

Example:

- Features: age, college GPA, state of residence
- Label: salary

Regression

- When the label is a continuous number, we call it a regression problem.
- **Examples:** predicting salary

Classification

- When the label is one of a finite number of choices, we call it a classification problem.
- Examples: predicting species, predicting gestures

Binary vs. Multiclass Classification

- In binary classification, there are only two possible labels.
- In multiclass classification, there are more than two possible labels.
- ► For simplicity, we'll focus on binary classification.

Features

- Features are most often numerical.
- ► Why?
 - 1. Computers process numbers (not penguins).
 - 2. Allows us to use mathematical machinery.

Feature Vectors

We often package features into a feature vector.

Example:

 \vec{x} = (bill length, body mass)^T

The dimensionality of a feature vector is the number of features it contains.

Choosing Features

- Features should contain information relevant to predicting the label.
- There should be a relationship between them.
 It might be quite complex!
- Choosing good features is crucial.
 "Garbage in, garbage out."

Learning from Data

- To teach the computer, we provide it with many training examples.
- Each example consists of an input feature vector x and the correct output label y.
- The set of examples is called the training set:

$$\mathcal{X} = \{(\vec{x}^{(1)}, y_1), \, (\vec{x}^{(2)}, y_2), \, \dots, \, (\vec{x}^{(n)}, y_n)\}$$

Learning from Data

- Hope: given enough examples, the computer will detect a pattern between the features and labels.
- ► This process is called **learning**.
- The more complex the relationship, the more examples we'll need.

Train Error

- To see how well the computer has learned, we can compute the train error.
 - Make predictions on the training set.
 - E.g., for classification, the fraction of training examples misclassified.
- But this is not always a good indicator of how well the computer will do on **new** examples.

Test Error

Instead, we reserve some examples for a test set.

Randomly choose, say, 30% of the examples to be in the test set.

training data (70%)	test data (30%)
---------------------	-----------------

Randomizing is important!

Test Error

- Train **only** on the training set.
- Make predictions on the test set.
- The error on the test set is the test error.
- The test error is a better indicator of how well the computer will do on new examples.

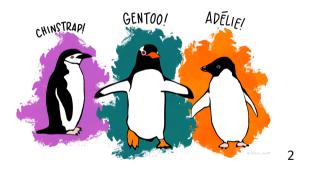
Generalization

- The ability of the model to perform well on new, unseen examples is called generalization.
- ▶ In prediction, it's what we're after.
- Training error can be useful, but we care mostly about test error.

Overfitting and Underfitting

- Overfitting: model does not generalize.
 Train error is much lower than test error.
- Underfitting: model is not learning the pattern.
 - Both train and test error are high.
 - Need more features, more complex model, etc.

Example: Penguin Prediction



Task: given bill length and body mass, predict species.

²Artwork by @allison_horst

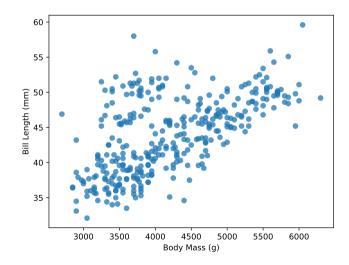
Training Set

- We collect a training set of 344 penguins. For each penguin, we record:
 - The features: bill length, body mass
 - The label: species
- Each penguin becomes a feature vector in \mathbb{R}^2 .

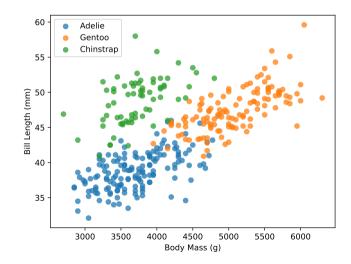
 $\vec{x}^{(i)}$ = (body mass of penguin *i*, bill length of penguin *i*)^{*T*}

• We can **embed** penguins as **point cloud** in \mathbb{R}^2 .

Penguin Embedding

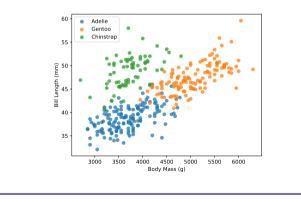


Penguin Embedding



Exercise

We see a new penguin with body mass of 5300 g and bill length of 46 mm. What is its species, most likely?



A Simple Intuition

- New penguin's embedding is close to Gentoo penguins ⇒ it is mostly likely also Gentoo.
- Our Assumption: locality. Nearby (similar) feature vectors have similar labels.



Lecture 01 | Part 3

Nearest Neighbors Predictors

Nearest Neighbors Predictors

- Idea: to predict the label of a new example:
 1. find the most similar example in the training set
 2. predict the same label
- This is called a nearest neighbor predictor.
- Useful for both regression and classification.

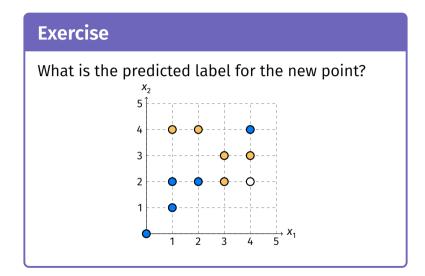
Nearest Neighbor Classifier

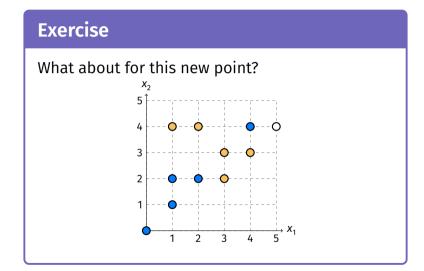
- **Data:** a training set \mathcal{X} of *n* feature vectors with labels: $\{(\vec{x}^{(i)}, y_i)\} = \{(\vec{x}^{(1)}, y_1), \dots, (\vec{x}^{(n)}, y_n)\}$
- **Given:** a new point, \vec{z} with unknown label.
- Predict:

1. Find the closest point to \vec{z} in \mathcal{X} :

$$i^* = \argmin_{i \in \{1, \dots, n\}} \| \vec{x}^{(i)} - \vec{z} \|$$

2. Use y_{i^*} as the predicted label.





A Note About Distances

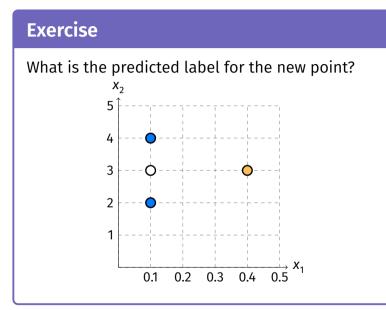
We found the nearest neighbor using the Euclidean distance:

$$\begin{split} \vec{p} - \vec{q} \parallel &= \sqrt{(p_1 - q_1)^2 + \dots + (p_d - q_d)^2} \\ &= \sqrt{\sum_{k=1}^d (p_k - q_k)^2} \\ &= \sqrt{(\vec{p} - \vec{q}) \cdot (\vec{p} - \vec{q})} \end{split}$$

Note that this is just one choice – there are other valid distances. E.g., cosine distance.

A Note About Distances

- The Euclidean distance treats all features equally.
- In other words, all features contribute equally to the prediction.



Standardizing Features

- When features are measured on different scales, it can help to standardize.
- Idea: shift and scale to make each feature have mean 0 and standard deviation 1.

Standardizing Features

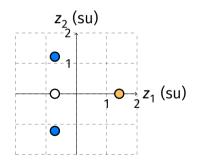
- Suppose we have two features, x₁ and x₂, and let:
 μ₁, μ₂ be the means of each feature in the training set,
 σ₁, σ₂ be the standard deviations.
- When standardizing:

$$(x_1, x_2)^T$$
 becomes $(z_1, z_2)^T = \left(\frac{x_1 - \mu_1}{\sigma_1}, \frac{x_2 - \mu_2}{\sigma_2}\right)^T$

Do this for all training data, and new test examples.

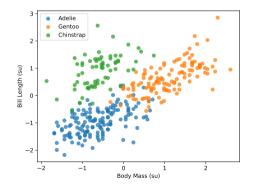
Example

When plotted in standard units, the data now looks like this:



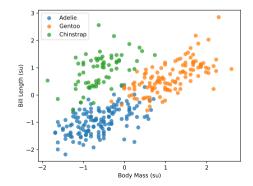
The Decision Boundary

We can visualize the prediction for every possible input.
 Decision boundary: where the prediction changes.

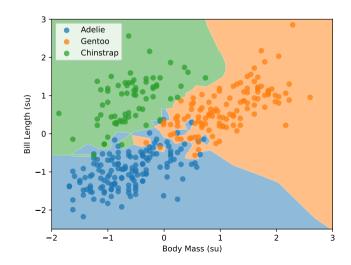


Exercise

What will the decision boundary look like for our NN penguin classifier, roughly-speaking?



The Decision Boundary



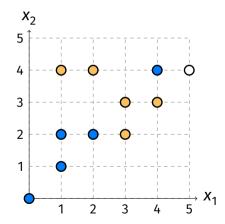
Exercise

Suppose there are no duplicates in the training data.

True or False: the nearest neighbor classifier will have 100% accuracy.

Problem

What if the nearest neighbor is an **outlier**?

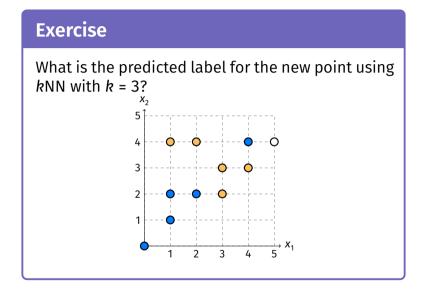


k-Nearest Neighbors

- Before: single closest neighbor determined prediction.
- Idea: have k closest neighbors "vote".
- Can be useful to reduce noise.

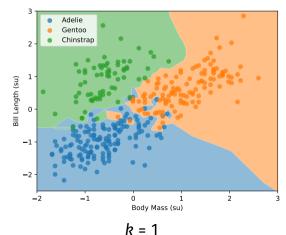
k-Nearest Neighbors Classifier

- **Data:** a training set \mathcal{X} of *n* feature vectors with labels: $\{(\vec{x}^{(i)}, y_i)\} = \{(\vec{x}^{(1)}, y_1), \dots, (\vec{x}^{(n)}, y_n)\}$
- Given: a new point, ż with unknown label, a choice for the parameter k.
- Predict:
 - 1. Find the *k* closest points to \vec{z} in \mathcal{X} :
 - 2. Use the most common label among those *k* points as the predicted label.



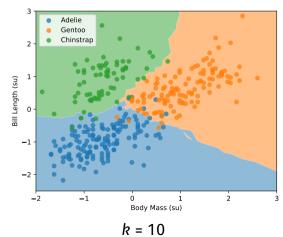
k and the Decision Boundary

How might the decision boundary change as we increase k?



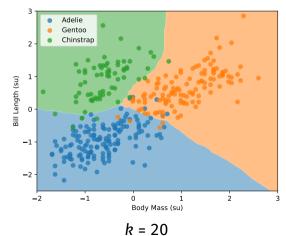
k and the Decision Boundary

How might the decision boundary change as we increase k?



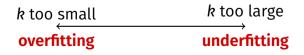
k and the Decision Boundary

How might the decision boundary change as we increase k?



k and "Complexity"

- k controls the "complexity" of the decision boundary.
- The larger k, the simpler the boundary.
- Choosing k appropriately controls overfitting/underfitting.



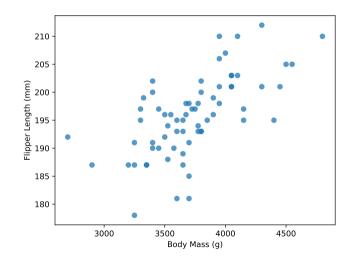
Exercise

What will the prediction be if we set k = n, where n is the number of training examples?

Nearest Neighbor Regression

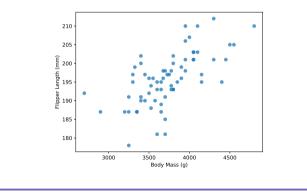
The nearest neighbor rule can be used for regression, too.

Motivation



Exercise

We see a new penguin with body mass of 4000 g. What is a likely flipper length for this penguin?



A Simple Prediction Algorithm

- Data: a set of penguins (as feature vectors) and their flipper lengths.
- Given: a new penguin whose flipper length is unknown.

Predict:

- 1. Find the *nearest* penguin whose flipper length is known.
- 2. Use that penguin's flipper length as our prediction.

Nearest Neighbor Regression

- **Data:** a set \mathcal{X} of *n* feature vectors with targets: $\{(\vec{x}^{(i)}, y_i)\} = \{(\vec{x}^{(1)}, y_1), \dots, (\vec{x}^{(n)}, y_n)\}$
- **Given:** a new point, \vec{z} with unknown target.

Predict:

1. Find the closest point to \vec{z} in \mathcal{X} :

$$i^* = \underset{i \in \{1, \dots, n\}}{\operatorname{arg\,min}} \left\| \vec{x}^{(i)} - \vec{z} \right\|$$

2. Use y_{i^*} as the predicted target.

kNN Regression

- As with classification, can generalize to k nearest neighbors.
- Natural prediction: the mean of the targets of the k closest neighbors.

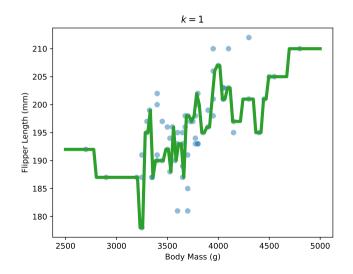
k-Nearest Neighbors Regression

- **Data:** a set \mathcal{X} of *n* feature vectors with targets: $\{(\vec{x}^{(i)}, y_i)\} = \{(\vec{x}^{(1)}, y_1), \dots, (\vec{x}^{(n)}, y_n)\}$
- **Given:** a new point, *z* with unknown target.

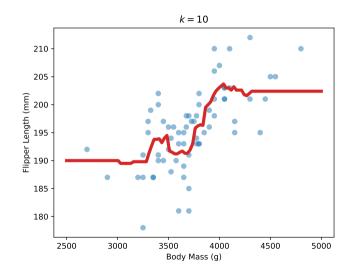
Predict:

- 1. Find the *k* closest points to \vec{z} in \mathcal{X}
- 2. Use the average of their labels as the predicted target

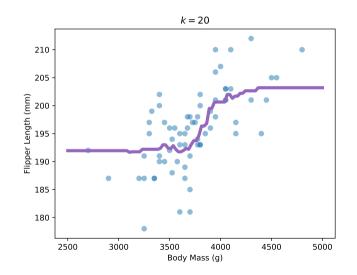
Example: *kNN* **Penguin Regression**



Example: *kNN* **Penguin Regression**



Example: *kNN* **Penguin Regression**





Lecture 01 | Part 4

Gesture Recognition Demo, Revisited

Gesture Recognition

The gesture recognition demo we saw earlier is a kNN classifier.

Features

- Each video frame is made into a *d*-dimensional feature vector.
 - 1. Converted to grayscale.
 - 2. Divided into *d* horizontal strips.
 - 3. Feature *i* is the average brightness of strip *i*.

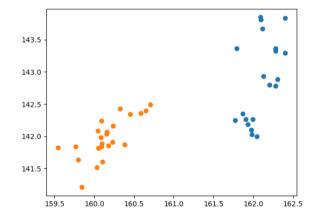
Example: *d* = 2



Example: *d* = 2



Example: *d* = 2



Observation

- The feature vectors for the same gesture are close together.
- ► The data has "organized" itself.

Prediction

Given a new frame, convert it to a feature vector and find the k closest training frames.

Beyond *d* = 2

- We can use more features.
 - ▶ We can still apply *k*NN in high dimensions.
 - (But we can't visualize the feature vectors with a scatter plot)
- The original demo used d = 5 features.

d = 5



Takeaway

Even seemingly-intelligent behavior can be achieved with simple algorithms + data.



Lecture 01 | Part 5

From Theory to Practice

Tip #0: Implementation

- sklearn has a kNN implementation.
- sklearn.neighbors.KNeighborsClassifier for classification.
- But this a theory class; we'll implement it ourselves.

Tip #0: Implementation

- kNN can be implemented in a few lines of code with numpy.
- useful functions:
 - np.linalg.norm: computes distances,
 - np.argmin: finds index of the minimum value
 - np.argpartition: finds indices of k smallest values
 - np.bincount: counts occurrences of each value

import numpy as np

```
def knn_predict(X_train, y_train, x, k=1):
    # compute distances between test and training examples
    distances = np.linalg.norm(X_train - x, axis=1)
```

find the indices of the k smallest distances nearest = np.argpartition(distances, k, axis=0)[:k]

```
# get the labels of the k nearest neighbors
nearest_labels = y_train[nearest]
```

```
# return the most common label
return np.bincount(nearest_labels).argmax()
```

Tip #1: Choosing k

To choose k, further divide your data into training, test, and validation sets.

train	test	val.]
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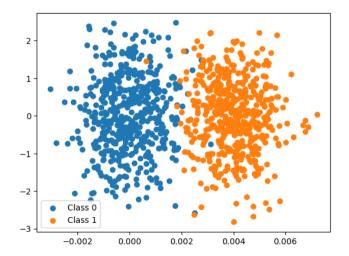
Tip #1: Choosing *k*

- Pick a few different values of k, train model on each, and compute error on the validation set.
- Keep the k that gives the lowest error; this is your choice.
- Compute test error using this *k*.

Tip #1: Choosing *k*

- When you're done and ready to use the model "in production":
 - 1. combine all of your data into one large training set,
 - 2. use the *k* you chose in validation,
 - 3. train the final model.

Tip #2: Standardizing Features



>> knn = sklearn.neighbors.KNeighborsClassifier(n_neighbors=1)
>> knn.fit(X_train, y_train)
>> knn.score(X_test, y_test)
0.672

```
>> mu, sigma = X_train.mean(axis=0), X_train.std(axis=0)
>> Z_train = (X_train - mu) / sigma
>> Z_test = (X_test - mu) / sigma
>> knn.fit(Z_train, y_train)
>> knn.score(Z_test, y_test)
0.972
```

Trivia: Speeding it Up

- Making a prediction requires computing the distance to every training example.
- There are ways of speeding this up:
 - Approximate nearest neighbors,
 - k-d trees, ball trees, etc.
 - Subsampling the data.



Lecture 01 | Part 6

The End?

The End?

- We have developed a simple prediction algorithm: k-nearest neighbors.
- Can used for both classification and regression.
- Often works well!
- Have we "solved" machine learning?

No

- Nearest neighbor predictors have significant limitations in two areas:
- 1. Computational efficiency
 - ▶ I.e., they are slow, or require a lot of memory.

2. Predictive performance

I.e., they aren't always as accurate as other methods.

Something Unsatisfying

- Do nearest neighbor models learn anything?
- They seem to just "memorize" the training data.

The Main Problem

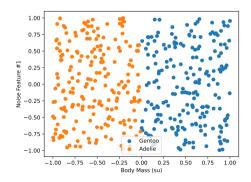
Nearest neighbor approaches do not learn which features are useful and which are not.

Example

- Suppose all Adelie penguins weigh less than all Gentoo penguins.
- I.e., we can predict perfectly based on body mass alone.

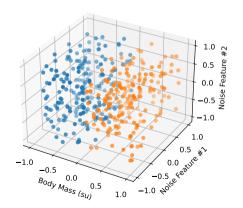
Example: One Noisy Feature

- Suppose we add a feature that is total noise.
- Still enough information to perfectly classify.
- ▶ 1-NN: 98% test accuracy.



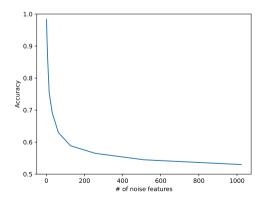
Example: Two Noisy Features

- Suppose we add another feature that is total noise.
- Still enough information to perfectly classify.
- 1-NN: 95% test accuracy (-3%).



Example: Noisy Features

- No matter how many noisy features we add, there is enough information to classify perfectly.
- But 1-NN performance degrades with # of (noisy) features:



Explanation

Euclidean distance treats all features the same. Even those that are pure noise.

- NN does not **learn** which features are useful.³
- Distance becomes less meaningful as noisy features are added.

³For extensions of kNN which learn a distance metric from data, see: (Weinberger and Saul, 2009; Goldberger et al., 2005; Shalev-Shwartz et al., 2004)

Summary

- kNN prediction is simple and can work well.
- It may be computationally intensive.
- It does not:
 - "learn" in the sense of "compressing knowledge".
 - learn which features are useful.

Next time...

A different approach that attempts to learn a "weight" for each feature.